Mobile Robot Self-Driving Through Image Classification Using Discriminative Learning of Sum-Product Networks

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Sum-Product Networks

Definition 1 (Gens and Domingos 2013).

A sum-product network (SPN) is a DAG where each node can be defined recursively as follows.

- 1. A tractable univariate probability distribution is an SPN.
- 2. A product of SPNs with disjoint scopes is an SPN.
- 3. A weighted sum of SPNs with the same scope is an SPN, provided all weights are positive.
- 4. Nothing else is an SPN.

Sum-product network

The value S(X) of an SPN is equal to $\phi(X)$, an unnormalized probability function, if it obeys certain properties. If all weights sum to one, $S(X) = P_{\phi}(X)$ (Poon and Domingos 2011).



Probability of evidence

Single backward pass computes $S(X = {X_1 = 0}) = 0.31$. Linear on the number of edges



Maximum a posteriori probability

Replace sums with max nodes. Backward pass followed by forward pass computes most probable explanation, i.e. find $\arg \max_{x \in X} P(X, E)$.



Learning

Structure

- PD-Dense architecture (Poon and Domingos 2011)
- Clustering on Variables (Dennis and Ventura 2012)
- Gens-Domingos LearnSPN (Gens and Domingos 2013)
- Using deep learning techniques (Peharz et al. 2018)
- many others...

Weights

- Generative and discriminative gradient descent
- Generative Expectation-Maximization
- Extended Baum-Welch (Rashwan, Poupart, and Zhitang 2018)
- many others...

Self-Driving



Dataset used: Moraes and Salvatore 2018



Lane tracking dataset with 80 \times 45 RGB images. Each labeled with either UP, LEFT or RIGHT.

Self-driving as image classification

Let $X = \{X_0, X_1, \dots, X_{n-1}\}$ be an **image**. Every $X_i = x_i$ refers to the *i*-th pixel with a grayscale intensity of x_i .

Let $Y = \{UP, LEFT, RIGHT\}$ be the classification variable.



The entire scope of variables is $X \cup \{Y\}$.

Objective: arg max_{$y \in Y$} P(Y = y|X)

Pipeline:

original RGB image \rightarrow grayscale \rightarrow some *T* transformation.

Three transformations tested:

- 1. Otsu binarization (Otsu 1979)
- 2. Quantization (resolution downscaling)
- 3. Histogram equalization



1



2



Raspberry Pi 3 Model B — Berry

 $\textbf{CPU:} \ \ \mathsf{Quad} \ \ \mathsf{Core} \ \ 1.2\mathsf{GHz} \ \ \mathsf{Broadcom} \ \ \mathsf{BCM2837} \ \ \mathsf{64bit} \ \ \mathsf{ARMv7}$

Memory: 1GB RAM

Storage: 16GB SSD



Lego Mindstorms NXT v2 — Brick

CPU: Atmel AT91SAM7S256 48MHz 32bit ARMv4

Memory: 64KB RAM

Storage: 256KB Flash



Robot

Berry handles inference, passing predicted label to Brick.

Brick handles motors according to label received from Berry.



Message passing through USB cable.

Driving with SPNs

Every pixel X_i is a variable in the distribution represented by the SPN, i.e. no additional feature extraction, end-to-end.

Two architectures:

GD: LearnSPN (Gens and Domingos 2013)

DV: Clustering on Variables (Dennis and Ventura 2012)

Three weight setups:

- g: Generative gradient descent (Poon and Domingos 2011)
- d: Discriminative gradient descent (Gens and Domingos 2012)
- s: Proportional weights for GD, random weights for DV

Accuracy

Accuracy (%)	DV+g	DV+d	DV+s	GD+g	GD+d	GD+s
В	78.8	78.8	78.8	82.8	83.8	85.0
Q_2	78.6	78.0	78.0	78.6	80.4	79.4
$Q_2 + E$	76.6	76.6	76.8	79.6	82.8	81.8
Q_3	77.4	77.4	77.4	77.6	80.2	79.8
$Q_3 + E$	70.4	76.6	76.6	79.2	81.2	77.4
Q_4	78.2	78.4	78.2	76.0	78.2	76.4
$Q_4 + E$	76.6	76.6	76.8	76.0	74.6	80.6
Q_5	77.8	78.4	78.4	77.6	74.0	73.8
$Q_5 + E$	76.6	76.6	76.6	72.0	72.8	72.0
Q_6	77.4	78.4	78.4	75.2	74.4	72.0
$Q_6 + E$	76.0	76.4	76.4	73.0	75.0	73.6
Q_7	78.2	78.4	78.4	62.8	72.2	71.4
$Q_7 + E$	76.2	76.4	76.4	70.6	71.4	71.6
Ø	78.0	78.4	78.4	62.4	62.4	62.4
Ε	76.4	76.4	76.4	60.4	60.0	61.2

Inference time

Inference (secs)	DV+g	DV+d	DV+s	GD+g	GD+d	GD+s
В	0.23	0.25	0.25	0.38	0.37	0.31
Q_2	0.22	0.24	0.23	0.28	0.34	0.16
$Q_2 + E$	0.22	0.23	0.23	0.38	0.30	0.27
Q_3	0.22	0.23	0.22	0.22	0.32	0.17
$Q_3 + E$	0.22	0.23	0.22	0.34	0.32	0.31
Q_4	0.22	0.22	0.23	0.16	0.17	0.13
$Q_4 + E$	0.23	0.27	0.29	0.13	0.14	0.13
Q_5	0.22	0.26	0.28	0.07	0.05	0.02
$Q_5 + E$	0.22	0.29	0.25	0.05	0.05	0.02
Q_6	0.23	0.24	0.23	0.04	0.05	0.01
$Q_6 + E$	0.22	0.24	0.28	0.03	0.04	0.02
Q_7	0.23	0.23	0.26	0.03	0.01	0.01
$Q_7 + E$	0.22	0.26	0.24	0.01	0.01	0.01
Ø	0.22	0.26	0.23	0.02	0.01	0.01
E	0.23	0.23	0.22	0.01	0.01	0.02

Model 1: Q_4 , GD+d Accuracy: 78.2% Desktop time: 170ms Berry time: 700ms Model 2: Q_6 , GD+d **Accuracy:** 74.4% **Desktop time:** 50ms Berry time: 150ms Model 3: \emptyset , GD+d **Accuracy:** 62.4% **Desktop time:** < 10ms Berry time: 75ms

Mobile Robot Self-Driving Through Image Classification Using Discriminative Learning of Sum-Product Networks — YouTube (https://youtu.be/vhpWQDX2cQU)

Inference and learning: GoSPN (https://github.com/RenatoGeh/gospn)

Mobile robot implementation: GoDrive (https://github.com/RenatoGeh/godrive)

Thank you.

Questions?

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