



**MAT0147 — CÁLCULO DIFERENCIAL E INTEGRAL II  
PARA ECONOMIA**

**GRÁFICOS DE FUNÇÕES DE DUAS VARIÁVEIS**

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Abaixo você encontra os gráficos das funções do Exercício 8, lista 2, e alguns outros interessantes. Repare na **orientação** dos eixos coordenados, que pode mudar de um gráfico para o outro.

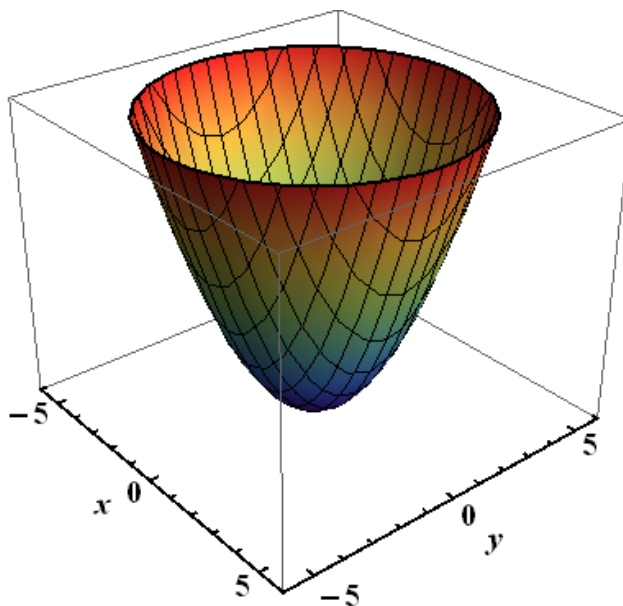
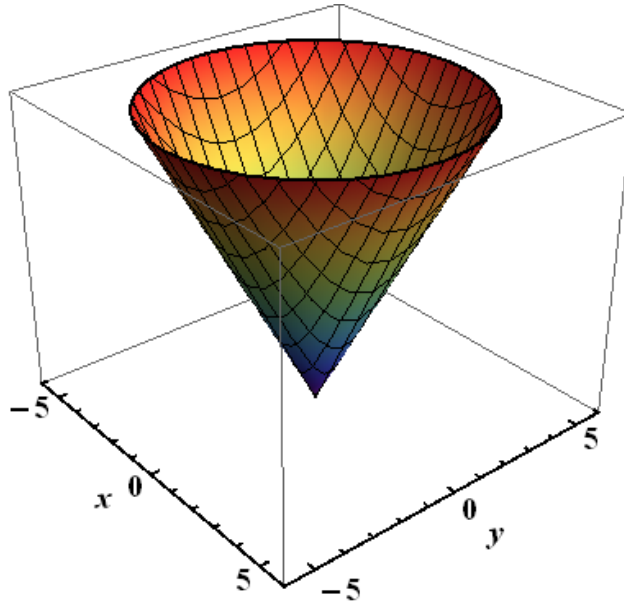
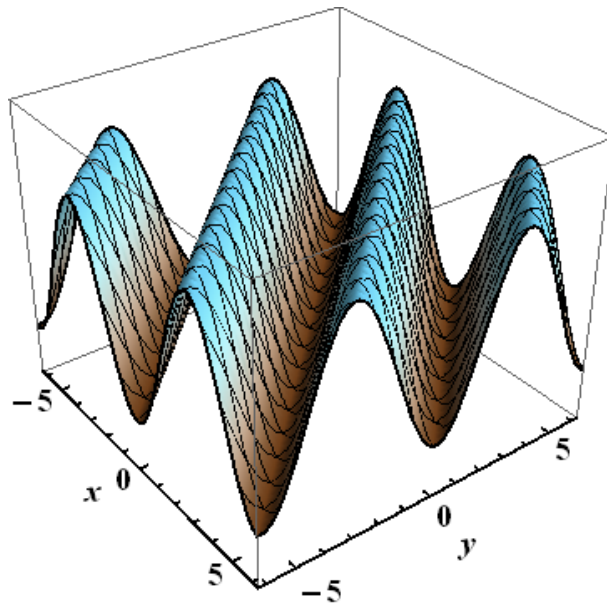


Gráfico de  $f(x, y) = x^2 + y^2$



**Gráfico de  $f(x, y) = \sqrt{x^2 + y^2}$**



**Gráfico de  $f(x, y) = \text{sen}(x + y)$**

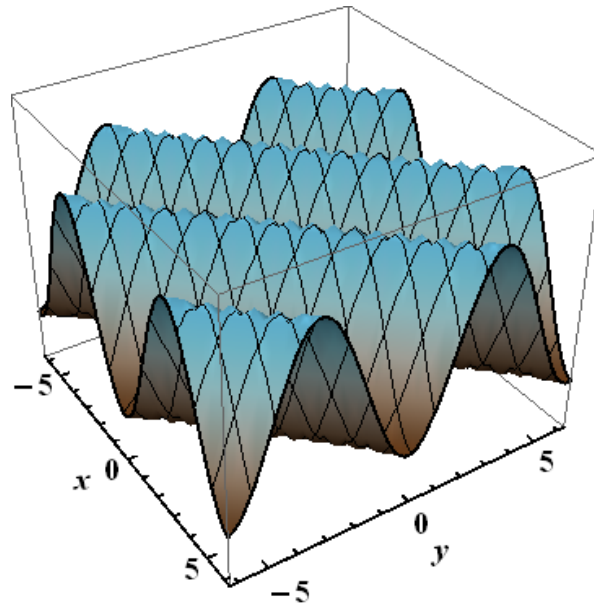


Gráfico de  $f(x, y) = \text{sen}(x - y)$

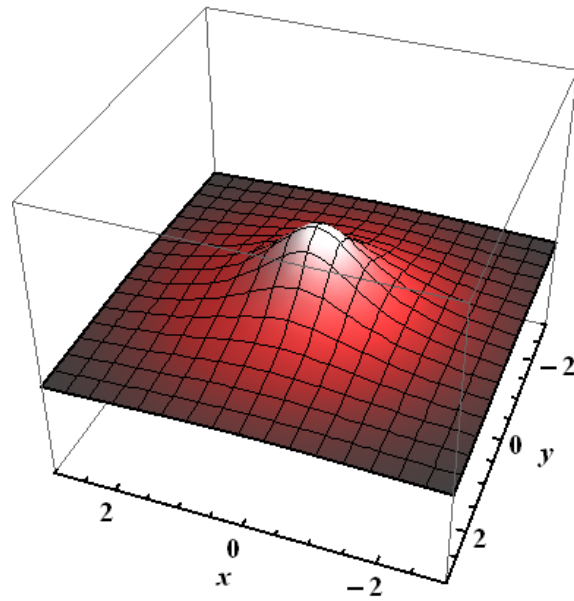
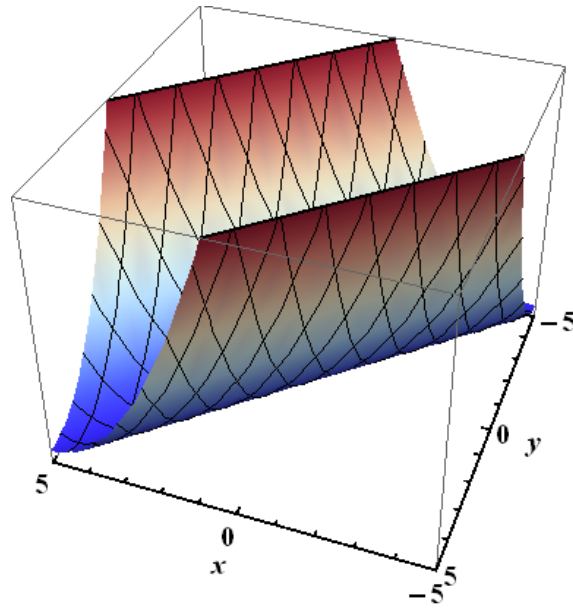
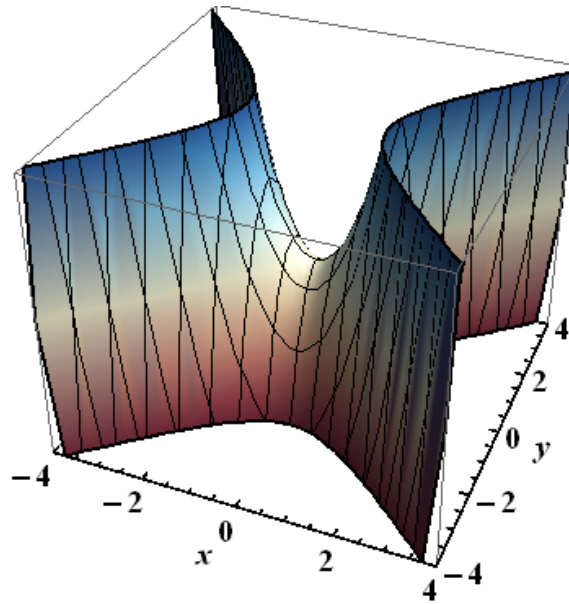


Gráfico de  $f(x, y) = \frac{1}{1 + x^2 + y^2}$



**Gráfico de  $f(x, y) = (x - y)^2$**



**Gráfico de  $f(x, y) = x^2 - y^2$**

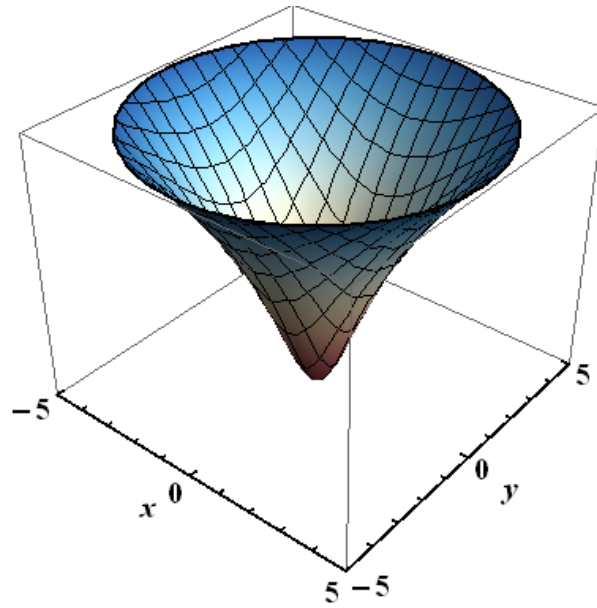


Gráfico de  $f(x, y) = \ln(1 + x^2 + y^2)$

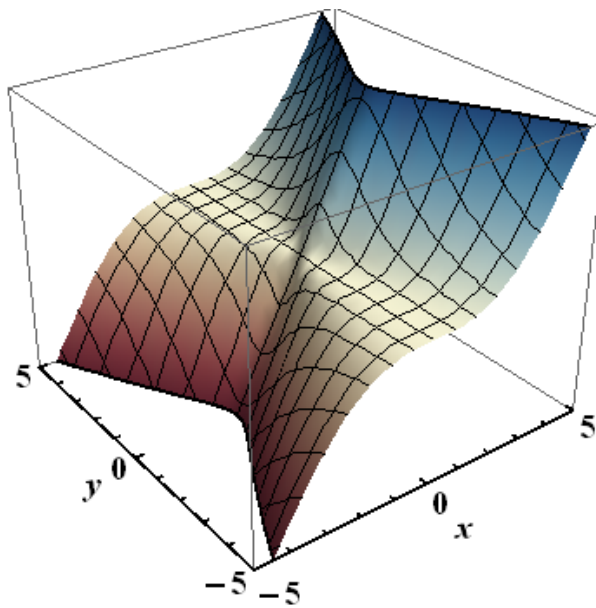
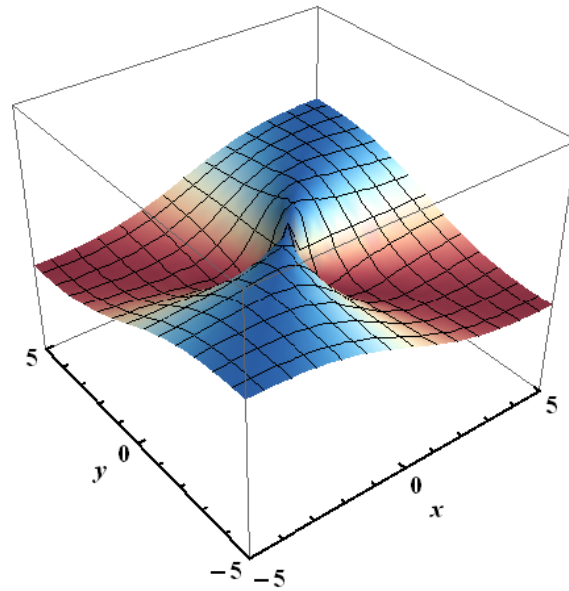


Gráfico de  $f(x, y) = \frac{x^3}{x^2 + y^2}$



**Gráfico de**  $f(x, y) = \frac{xy}{x^2 + y^2}$

Repare neste último gráfico a descontinuidade em  $(0, 0)$ : indo pelo caminho  $x = y$ , a função fica constante igual a  $\frac{1}{2}$  (em azul), logo tende a  $\frac{1}{2}$ .

Pelo caminho  $x = -y$ , ela fica constante igual a  $-\frac{1}{2}$  (em vermelho) e tende a esse valor.