

**MAT216 – Cálculo Diferencial e Integral III**  
**Respostas da Lista de Exercícios 1**

2.  $f(x, y) = x^2 - x$ .
5. (a)  $f_x = y^2/(x^2 + y^2)^{3/2}$ ,  $f_y = -xy/(x^2 + y^2)^{3/2}$ . (b)  $f_{x_k} = 2 \sum_{i=1}^n a_{ki} x_i$ . (c)  $f_{x_k} = a_k$ . (d)  $f_{x_k} = 2x_k$ .
6. (a)  $a \cdot v/||v||$ . (b)  $2x \cdot v/||v||$ .
7. (a) Usar  $\frac{\partial f}{\partial(-v)}(p) = -\frac{\partial f}{\partial v}(p)$ . (b)  $f(x) = v \cdot x$ .
8. (a)  $(2x + y^3 \cos(xy), 2y \sin(xy) + xy^2 \cos(xy))$ . (b)  $e^x(\cos y, -\sin y)$ . (c)  $2(x, -y, z)$ .
9.  $-\sqrt{6}/3$ .
10. Pontos  $(-1, 0)$  e  $(1, 0)$  com direções  $(-1, 0)$  e  $(1, 0)$ , resp.
11.  $\nabla f(1, 2) = (2, 2)$ ;  $14/5$ .
12. (b)  $f(x, y, z) = (x^2 + y^2 + z^2)/2$ .
13. (a)  $-2/3$ . (b)  $0$ .
14.  $x + 2y - \sqrt{5}z = 0$ .
15.  $y_0 z_0 x + z_0 x_0 y + x_0 y_0 z = 3$ .
16.  $N_1 = (2, 4, -1)$ ,  $N_2 = (2, 6, -1)$ ,  $v = (2, 0, 4)$ ;  $v$  é tangente à curva intersecção  $S_1 \cap S_2$ .
17.  $x = t$ ,  $y = -2 + 3t$ ,  $z = 3 - 2t$  para  $t \in \mathbf{R}$ .
18. Valor aproximado 1. A calculadora fornece 0,98542.