

Fig. 1.7. Arrival phases from an earthquake (top) and explosion (bottom) at 40 points per second.

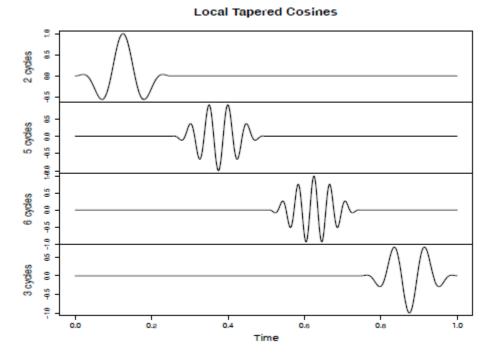


Fig. 4.19. Local, tapered cosines at various frequencies.

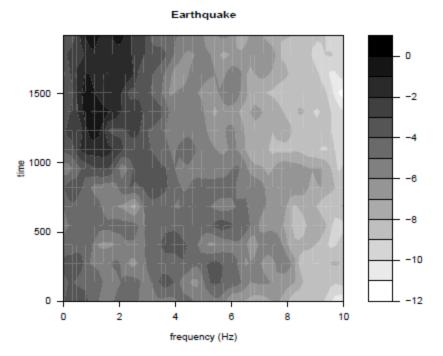


Fig. 4.17. Time-frequency image for the dynamic Fourier analysis of the earthquake series shown in Figure 1.7.

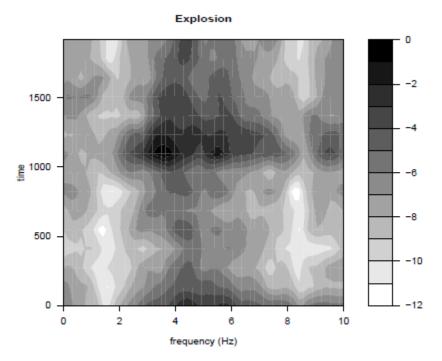


Fig. 4.18. Time-frequency image for the dynamic Fourier analysis of the explosion series shown in Figure 1.7.

in the images, darker areas correspond to higher power. Specifically, in this example, let  $x_t$ , for t = 1; ...; 2048, represent the series of interest. Then, the sections of the data that were analyzed were  $[x_{tk+1}; ...; x_{tk+256}]$ , for  $t_k = 128k$ , and k = 0; 1; ...; 14; e.g., the first section analyzed is  $\{x1; : : : ; x256\}$ , the second section analyzed is  $\{x129; : : : ; x384\}$ , and so on. Each section of 256 observations was tapered using a cosine bell, and spectral estimation was performed using a repeated Daniell kernel with weights  $1/9\{1; 2; 3; 2; 1\}$ .

The S component for the earthquake shows power at the low frequencies only, and the power remains strong for a long time. In contrast, the explosion shows power at higher frequencies than the earthquake, and the power of the signals (P and S waves) does not last as long as in the case of the earthquake.

## Earthquake

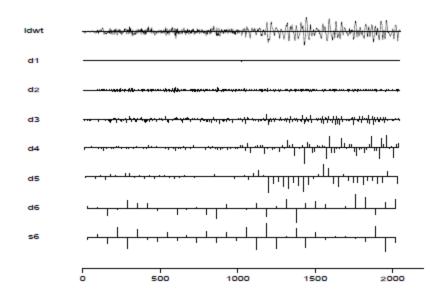


Fig. 4.22. Discrete wavelet transform of the earthquake series using the symmlet8 wavelets, and J = 6 levels of scale.

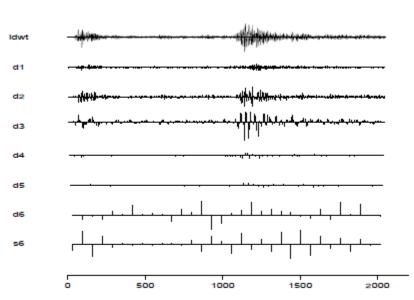


Fig. 4.23. Discrete wavelet transform of the explosion series using the symmlet8 wavelets and J = 6 levels of scale.

## Explosion

Comparing the DWTs, the earthquake is best represented by wavelets with larger scale than the explosion. One way to measure the importance of each level,  $d1, d2, \ldots, d6, s6$ , is to evaluate the proportion of the total power (or energy) explained by each. The total power of a time series  $x_t$ , for  $t = 1, \ldots, n$ , is  $TP = \sum_{t=1}^{n} x_t^2$ . The total power associated with each level of scale is (recall  $n = 2^{11}$ ),

$$TP_6^s = \sum_{k=1}^{n/2^6} s_{6,k}^2$$
 and  $TP_j^d = \sum_{k=1}^{n/2^j} d_{j,k}^2$ ,  $j = 1, \dots, 6$ .

Because we are working with an orthogonal basis, we have

$$TP = TP_6^s + \sum_{j=1}^{6} TP_j^d,$$

and the proportion of the total power explained by each level of detail would be the ratios  $TP_j^d/TP$  for j = 1, ..., 6, and for the smooth level, it would be  $TP_6^s/TP$ . These values are listed in Table 4.2. From that table nearly 80% of the total power of the earthquake series is explained by the higher scale details d4 and d5, whereas 90% of the total power is explained by the smaller scale details d2 and d3 for the explosion.

Component	Earthquake	Explosion
s6	0.009	0.002
d6	0.043	0.002
d5	0.377	0.007
d4	0.367	0.015
d3	0.160	0.559
d2	0.040	0.349
d1	0.003	0.066

Table 4.2. Fraction of Total Power

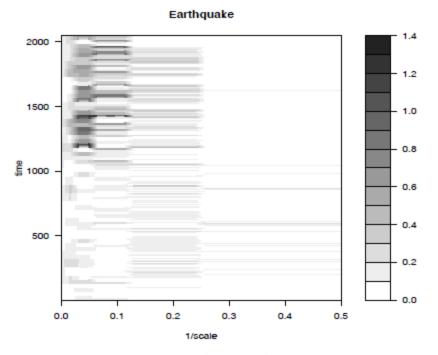
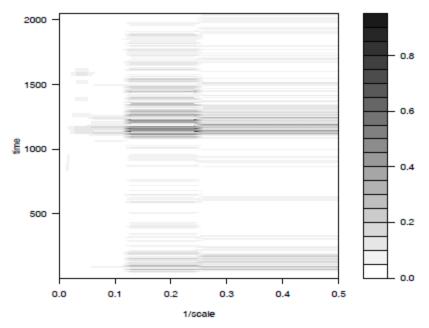


Fig. 4.24. Time-scale image (scalogram) of the earthquake series.



Explosion

Fig. 4.25. Time-scale image (scalogram) of the explosion series.

## Earthquake

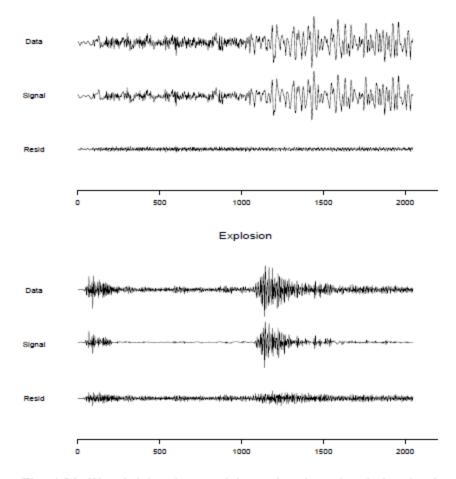


Fig. 4.26. Waveshrink estimates of the earthquake and explosion signals.