

1. Calcular a transformada de Laplace:

$$(a) f(t) = \cos(\omega t + \theta) \quad (1)$$

$$(b) f(t) = \cos(t) \sin(t) \quad (2)$$

2. Achar a transformada inversa:

$$(a) F(s) = \frac{s + 1}{s^3 + s^2 - 6s} \quad (3)$$

$$(b) F(s) = \frac{2}{s} + \frac{1}{s + 2} \quad (4)$$

$$(c) F(s) = \frac{1}{(s^2 + \omega^2)^2} \quad (5)$$

3. Resolver as equações diferenciais:

$$(a) \ddot{x} + \pi^2 x = t^3 \text{ com } x(0) = 6/\pi^4, \dot{x}(0) = 0 \quad (6)$$

$$(b) \ddot{x} + k\dot{x} - 2k^2 x = 0 \text{ com } x(0) = 2, \dot{x}(0) = 2k \quad (7)$$

$$(c) \ddot{x} - 2\dot{x} + x = \exp t + t \text{ com } x(0) = 0, \dot{x}(0) = 0 \quad (8)$$

$$(d) \ddot{x} + 2\dot{x} + 2x = r(t) \text{ com } x(0) = 0, \dot{x}(0) = 0 \quad (9)$$

$$r(t) = \begin{cases} t & \text{se } 0 < t \leq 1 \\ t^2 & \text{se } 1 < t \end{cases}$$

$$(e) \ddot{x} + 2\dot{x} - 3x = \delta(t - 2) + \delta(t - 3) \text{ com } x(0) = 0, \dot{x}(0) = 0 \quad (10)$$