

# Arkady Tsurkov

Classification of the quasi-varieties of the finitely generated  
nilpotent class 2 torsion free groups is a wild problem

or how the Universal Algebraic Geometry works.

Let  $F$  be a field.  $M_n(F)$  is the algebra of the  $n \times n$  matrices over  $F$ . We can consider the acting of the group  $GL_n(F)$  over set of  $k$ -tuples of matrices from  $M_n(F)$ :  $(A_1, \dots, A_k)^S = (S^{-1}A_1S, \dots, S^{-1}A_kS)$ , where  $S \in GL_n(F)$ . The problem of classification of the orbits of this action called wild problem if  $n, k \geq 2$ . This problem is unsolved and very difficult for infinite  $F$ . It will be proved that the problem of the classification of the quasi-varieties of the finitely generated nilpotent class 2 torsion free groups is not easier than the wild problem. The methods of the universal algebraic geometry will be actively used.