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$$p(\lambda) = \begin{vmatrix} (-4-\lambda) & 3 \\ 3 & (4-\lambda) \end{vmatrix} = -(16-\lambda^2) - 9$$

$$= \lambda^2 - 25 = (\lambda + 5)(\lambda - 5)$$

autovalores ± 5

$$\begin{bmatrix} -4 & 3 \\ 3 & 4 \end{bmatrix} \begin{bmatrix} x \\ 1 \end{bmatrix} = \begin{bmatrix} -4x + 3 \\ 3x + 4 \end{bmatrix} = \begin{bmatrix} 5x \\ 5 \end{bmatrix}$$

$$3x + 4 = 5 \quad \left| \text{para } \lambda = -5: \right.$$

$$3x = 1$$

$$x = \frac{1}{3}$$

$$3x + 4 = -5$$

$$3x = -9$$

$$x = -3$$

$$\begin{bmatrix} \frac{1}{3} \\ 1 \end{bmatrix} \text{ ou } \begin{bmatrix} 1 \\ 3 \end{bmatrix} \quad \longleftrightarrow \text{perpendicular!} \quad \begin{bmatrix} -3 \\ 1 \end{bmatrix}$$

$$\| (1, 3) \| = \| (-3, 1) \| = \sqrt{10}$$

$$\frac{1}{\sqrt{10}} \begin{bmatrix} 1 & -3 \\ 3 & 1 \end{bmatrix} = Q \text{ e' matriz ortogonal}$$

$$\text{então } Q^t Q = Q Q^t = I, \quad Q^t = Q^{-1}$$