

**MAT2454 - Cálculo Diferencial e Integral para Engenharia II**  
 Mais algumas respostas da 1<sup>a</sup> lista de exercícios - 2012

19. (a)  $\gamma : \mathbb{R} \rightarrow \mathbb{R}^2, \gamma(t) = (t, \frac{1}{2}(1-t))$

Reta tangente:  $X = (\frac{1}{2}, \frac{1}{4}) + \lambda(2, -1), \lambda \in \mathbb{R}$

(b)  $\gamma : [-\frac{\pi}{2}, \frac{\pi}{2}] \rightarrow \mathbb{R}^2, \gamma(t) = (5 + \cos(t), \frac{1}{\sqrt{2}} \sin(t))$

Reta tangente:  $X = (6, 0) + \lambda(1, 0), \lambda \in \mathbb{R}$

(c)  $\gamma_1 : ]-\frac{\pi}{2}, \frac{\pi}{2}[ \rightarrow \mathbb{R}^2, \gamma_1(t) = (\sec(t), \operatorname{tg}(t))$  parametriza um ramo da hipérbole

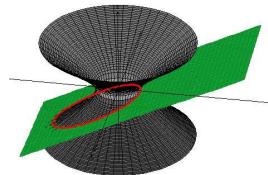
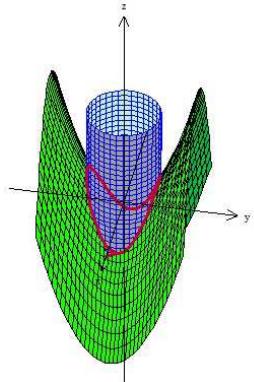
e

$\gamma_2 : ]\frac{\pi}{2}, \frac{3\pi}{2}[ \rightarrow \mathbb{R}^2, \gamma_2(t) = (\sec(t), \operatorname{tg}(t))$  parametriza o outro ramo.

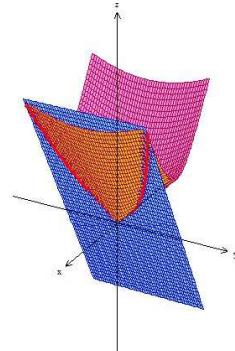
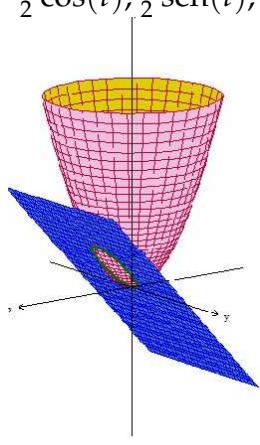
Reta tangente:  $X = (\sqrt{2}, 1) + \lambda(\sqrt{2}, 1), \lambda \in \mathbb{R}$

20.

(a)  $\gamma : [0, 2\pi] \rightarrow \mathbb{R}^3, \gamma(t) = (\cos(t), \sin(t), -\cos(2t))$       (b)  $\gamma : [0, 2\pi] \rightarrow \mathbb{R}^3, \gamma(t) = (\sqrt{2} \cos(t), 2 \sin(t) - 1, \sin(t) - 1)$



(c)  $\gamma : [0, 2\pi] \rightarrow \mathbb{R}^3, \gamma(t) = (\frac{1}{2} + \frac{1}{2} \cos(t), \frac{1}{2} \sin(t), \frac{1}{2} + \frac{1}{2} \cos(t))$       (d)  $\gamma : \mathbb{R} \rightarrow \mathbb{R}^3, \gamma(t) = (\frac{1}{4}(t^2 - 1), t, \frac{1}{2}(t^2 + 1))$

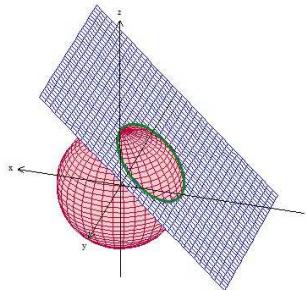


**21.**

(a)  $\gamma : [0, 2\pi] \rightarrow \mathbb{R}^3, \gamma(t) = (\frac{1}{2}(\cos(t) - 1), \frac{1}{\sqrt{2}} \sin(t), \frac{1}{2}(\cos(t) + 1))$

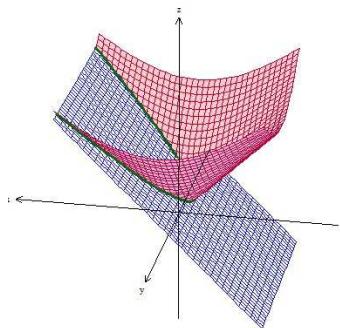
Nessa parametrização,  $\gamma(\frac{\pi}{2}) = (-\frac{1}{2}, \frac{\sqrt{2}}{2}, \frac{1}{2})$ , assim o vetor tangente à trajetória de  $\gamma$  nesse ponto é paralelo a  $\overline{\gamma}'(\frac{\pi}{2})$ .

Reta tangente:  $X = (-\frac{1}{2}, \frac{\sqrt{2}}{2}, \frac{1}{2}) + \lambda(-1, 0, -1), \lambda \in \mathbb{R}$



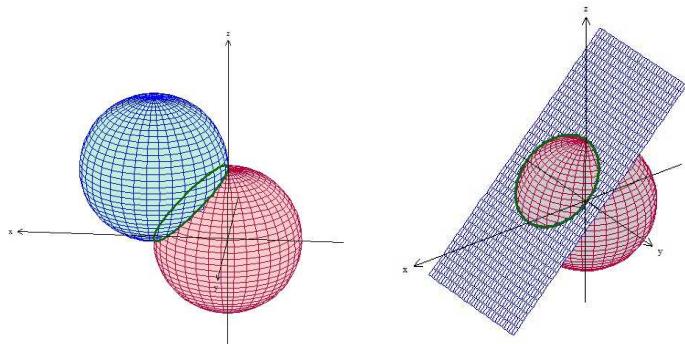
(b)  $\gamma : \mathbb{R} \rightarrow \mathbb{R}^3, \gamma(t) = (\frac{1}{2}(t^2 - 1), t, \frac{1}{2}(t^2 + 1))$

Reta tangente:  $X = (0, 1, 1) + \lambda(1, 1, 1), \lambda \in \mathbb{R}$



(c)  $\gamma : [0, 2\pi] \rightarrow \mathbb{R}^3, \gamma(t) = (\frac{1}{2}(1 - \cos(t)), \frac{1}{\sqrt{2}} \sin(t), \frac{1}{2}(\cos(t) + 1))$

Reta tangente:  $X = (\frac{1}{2}, \frac{\sqrt{2}}{2}, \frac{1}{2}) + \lambda(1, 0, -1), \lambda \in \mathbb{R}$



**22.** Veja a solução na P1 de 2009.